

Predicting Fluid Behaviour: The Power of Navier-Stokes Equations

Fluid dynamics is a branch of science that deals with the motion of gaseous and liquid substances and the phenomena occurring within them¹. It extends from sipping coffee swirled with milk to raging hurricanes. One of the most critical imperatives in comprehending flows is the Navier-Stokes equation, a time-honored mathematical formulation describing the formulations through which fluids behave with given forces². These equations count to decimal points in the format of controlling and predicting fluid motion under situations encountered, the worst of which are chaotic and turbulent.

Conservation of mass, conservation of momentum, and conservation of energy collectively form the basis of the Navier-Stokes equations³. Thus, the conservation of mass states that the mass cannot be produced or destroyed in the whole fluid. What enters the system remains inside or goes out of it. Conservation of momentum is held according to Newton's second law, which states that fluid accelerates when forces that act on them are made known. Like pressure, the troops may be gravity or viscosity. Conservation of energy shows how energy is conveyed by heat work and transferred to the internal energy system. Mathematically, partial derivatives and vector calculus are involved but very complicated governing saturation equations. However, it makes possible the evolution of velocity, pressure, and density parameters with time with moving fluids.

One of the most opposed sections of fluid dynamics is turbulence, characterized by unpredictable behavior and chaos during the flow. Still, an exact example can be smoke from a candle or the random movement of the air around the wing of an airplane. The movements involved can hardly be modeled precisely but can be modeled approximately using the Navier-Stokes equation. To solve the Navier-Stokes equations, scientists break the fluid motion into smaller regions and calculate the forces that act on them. These models are essential to understanding real-world problems where turbulence plays a key role.

¹ ScienceDirect. (n.d.). Fluid dynamics. Retrieved March 20, 2025, from <https://www.sciencedirect.com/topics/engineering/fluid-dynamics#:~:text=2.6%20Fluid%20dynamics,cost%20of%20devices%20and%20materials>

² Faro, A. A. (2020). Navier-Stokes Equation (An overview and the simplification). DOI:10.13140/RG.2.2.17406.00323.

³ SimScale. (n.d.). What are the Navier-Stokes equations?. Retrieved from <https://www.simscale.com/docs/simwiki/numerics-background/what-are-the-navier-stokes-equations/>

Weather forecasting is a significant application of the Navier-Stokes equations. The atmosphere may be considered a massive fluid system where wind currents, pressure differences, and temperature differences induce changes in weather patterns. Vast volumes of data are fed into numerical models based upon the Navier-Stokes equations by meteorologists to provide increasingly accurate forecasts of storms, rainfall, and climate trends. So also, the equations find their application in aerodynamics to a greater extent in the design of aircraft and automobiles. Engineers analyze the different interactions of airflow around the wings to lift and drag to develop an aircraft design and simulation based on the Navier-Stokes equations that will provide maximum lift and minimum drag. The same principle applies in road car manufacturing for aero improvement, increasing speed, and enhancing fuel economy.

These are further useful in oceanography. Ocean circulation also influences global climate patterns and marine ecosystems. Solving the Navier-Stokes equations for ocean circulation enables scientists to predict ocean circulation and how it affects weather, climate change, and environmental disasters like oil spills. Knowledge regarding these currents can benefit ecological protection and economic activity: shipping and fishing.

The Navier-Stokes equations are thought to describe both laminar and turbulent flow⁴. This can be shown simply by dropping ink into a glass of water: initially, the ink spreads laminar, whereas the turbulent flow sets in with the ring of the water. Despite achievements in computational fluid dynamics, turbulence continues to be one of the most studied but least understood phenomena in physics.

These Navier-Stokes equations are central to fluid motion studies, from storm predictions to aircraft design optimizations. While exact solutions remain out of reach, computational methods and simulations allow accurate predictions across numerous scientific fields. The next time you see clouds swirling across the sky or a river crashing onto some rocks, know then that you are observing the workings of fluid dynamics.

⁴ Dou, H.-S. (2022). No existence and smoothness of solution of the Navier-Stokes equation. *Entropy*, 24(3), 339. <https://doi.org/10.3390/e24030339>

References:

ScienceDirect. (n.d.). Fluid dynamics. Retrieved March 20, 2025, from <https://www.sciencedirect.com/topics/engineering/fluid-dynamics#:~:text=2.6%20Fluid%20dynamics,cost%20of%20devices%20and%20materials>

Faro, A. A. (2020). Navier-Stokes Equation (An overview and the simplification). DOI:10.13140/RG.2.2.17406.00323.

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